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目录

Coulomb's Law 库伦定律	2
Gauss's Law 高斯定律	5
Capacitance 电容	7

Peter MUYANG NI @ BNDS

Coulomb's Law 库伦定律

		点电荷	平板电容
库伦力 \vec{F}		$F = \frac{k q_1q_2 }{r^2}$	
电场强度 \vec{E}	$\vec{E} = \vec{F}/q_0$ (N/C)	$\vec{E} = \frac{kq}{r^2}\hat{r}$	
电势 V	$dV = -\vec{E} \cdot d\vec{l}$	$V = \frac{kq}{r}$	$V = -Ex$
电势能 U	$dU = -\vec{F} \cdot d\vec{l}$	$U_e = q_0V$	$U = -Fx = q_0V$

考点 1 ● 电荷是分正负的，不同电荷的电场/电势。 **Barron Ch11-2,3**

1. Which of the three charge distributions in the right figure has a point or points where the electric field is zero (not counting $\pm\infty$)?
 (A) I (B) II (C) III
 (D) I and II (E) I, II, and III

2. Which of the three distributions in figure above has a point or points where the potential is zero (excluding $\pm\infty$, but assuming that the potential equals zero at these latter points)?
 (A) I (B) II (C) III
 (D) I and II (E) I, II, and III

考点 2 ● 电荷是可以流动的。 **Barron Ch11-1**

Experiment I: A positively charged rod is brought near sphere A while the switch is closed, the switch is opened, and the rod is then removed.

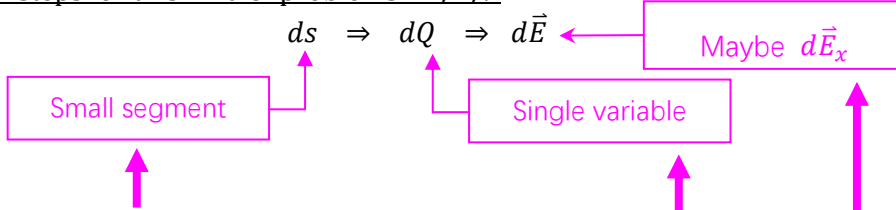
After experiment I
 sphere A is _____ negatively charged _____ positively charged
 sphere B is _____ negatively charged _____ positively charged

Experiment II: A positively charged rod is touched to sphere A while the switch is closed, the switch is opened, and the rod is then removed.

After experiment II
 sphere A is _____ negatively charged _____ positively charged
 sphere B is _____ negatively charged _____ positively charged

考点 1	1. 答案 E. 各种情况 $E=0$ 的点: I 在两电荷之间, II 在 -q 左边, III 在两电荷中间 2. 答案 B. 电势=0 的点在两电荷中间。
考点 2	I: sphere A <u>negatively</u> charged; sphere B <u>positively</u> charged II: sphere A <u>positively</u> charged; sphere B <u>positively</u> charged

General steps for this kind of problems: \vec{E}, \vec{F}, V



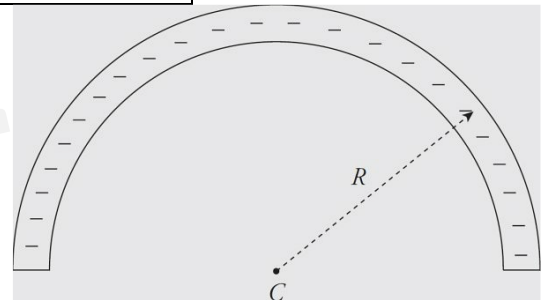
1D		
2D	$dA = 2\pi R dR$	area of a washer
3D	$dV = 4\pi R^2 dR$	volume of a spherical shell

1D	λ	$dQ = \lambda d(\text{length})$
2D	σ	$dQ = \sigma d(\text{area})$
3D	ρ	$dQ = \rho d(\text{volume})$

$d\vec{F} = k \frac{qdQ}{r^2} \vec{r}$	$\begin{cases} d\vec{E}_x = d\vec{E} \cos \theta \\ d\vec{E}_y = d\vec{E} \sin \theta \end{cases}$
$d\vec{E} = \frac{k dQ}{r^2} \vec{r}$	
$dV = \frac{k dQ}{r}$	

考点: ● 注意三个步骤，尤其最后一步 $d\vec{E}$ 可能是只计算 $d\vec{E}_x$ 或者 $d\vec{E}_y$

Example: A thin, nonconducting rod that carries a uniform linear charge Q^- is bent into a semicircle of radius R . Find the electric field at the center of curvature of the semicircle.



Step 1: find ds

λ is the linear charge density:

$$\lambda = Q/\pi R$$

Divide the semicircle into infinitesimal segments ds ,

$$ds = R d\theta$$

Step 2: $dQ \Rightarrow$ single variable that you integrate with respect to.

The charge in a segment of length ds is dQ

$$dQ = \lambda ds = \frac{Q}{\pi R} R d\theta = \frac{Q}{\pi} d\theta$$

Step 3: Find the differential function: $d\vec{E}$

As the ring is symmetry, the net field \vec{E} at center of curvature is along the y-axis:

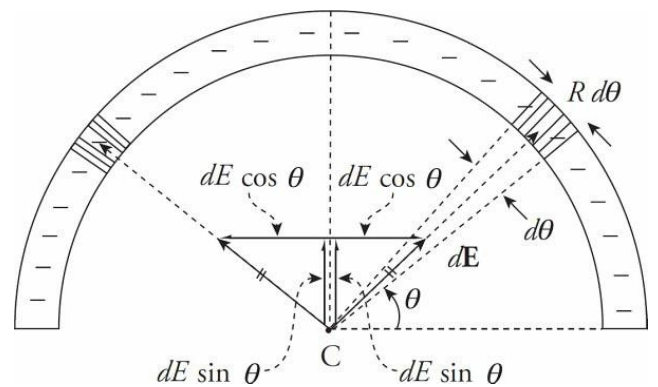
$$\vec{E} = E_y \vec{j}$$

The distance from the segment ds to the center is R :

$$dE_y = dE \sin \theta = \left(\frac{k}{R^2} dQ \right) \sin \theta = \left(\frac{k}{R^2} \frac{Q}{\pi} d\theta \right) \sin \theta$$

$$E_y = \frac{kQ}{\pi R^2} \int_0^\pi \sin \theta d\theta = \frac{kQ}{\pi R^2} (-\cos \theta)_0^\pi = \frac{2kQ}{\pi R^2}$$

$$\vec{E} = E_y \vec{j} = \frac{2kQ}{\pi R^2} \vec{j}$$



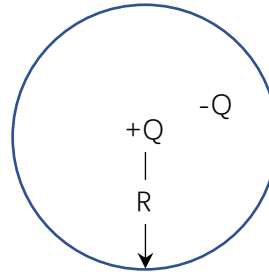
Please notice that only θ in the equation is a variable; other factors are all constants. (single variable)

仅仅对 E_y 进行积分

考点:

- 电荷均匀分布的球体: 半径 r 外部的电荷对半径 r 表面电场无影响。

Example(AP-C HW-13-8): A negative charge $-Q$ is distributed throughout the spherical volume of radius R shown by the equation $\rho=kr$, $r<R$. A positive point charge $+Q$ is at the center of the sphere. Determine each of the following in terms of the quantities given and fundamental constants.



a. The constant k .

半径为 r , 厚度为 dr 的空心球体积为 $dV = 4\pi r^2 dr$,
所含电荷 $dQ = \rho dV = (kr)(4\pi r^2 dr) = 4k\pi r^3 dr$

$$\int_0^R 4k\pi r^3 dr = 4k\pi \frac{R^4}{4} = Q \Rightarrow k = Q/\pi R^4$$

b. The electric field E outside the sphere at a distance $r>R$ from the center

$$\text{当 } r > R \text{ 时 } +Q \text{ 产生的电场 } \vec{E}_+ = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$

$$\text{当 } r > R \text{ 时 } -Q \text{ 产生的电场 } \vec{E}_- = \frac{-Q}{4\pi\epsilon_0 r^2} \hat{r}$$

$$\text{当 } r > R \text{ 时 } +Q \text{ 和 } -Q \text{ 的电场抵消 } \Sigma \vec{E} = 0$$

c. The electric potential V outside the sphere at a distance $r>R$ from the center

$$\text{当 } r > R \text{ 时 } +Q \text{ 产生的势能 } V_+ = \frac{Q}{4\pi\epsilon_0 r}$$

$$\text{当 } r > R \text{ 时 } -Q \text{ 产生的势能 } V_- = \frac{-Q}{4\pi\epsilon_0 r}$$

$$\text{当 } r > R \text{ 时 } +Q \text{ 和 } -Q \text{ 的势能抵消 } \Sigma V = 0$$

d. The electric field E inside the sphere at a distance $r<R$ from the center

$$\text{当 } r < R \text{ 时 } +Q \text{ 产生的电场 } \vec{E}_+ = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$

$$\text{当 } r < R \text{ 时 } -Q \text{ 的电荷 } dQ = 4kr^3 dr = 4 \frac{Q}{R^4} r^3 dr$$

$$\Rightarrow Q_- = \int_0^r 4 \frac{Q}{R^4} r^3 dr = 4 \frac{Q}{R^4} \left(\frac{r^4}{4} \right) = \frac{r^4}{R^4} Q$$

$$\vec{E}_- = \frac{-Q}{4\pi\epsilon_0 r^2} \left(\frac{r^4}{R^4} \right) \hat{r}$$

$$\begin{aligned} \Sigma \vec{E} &= \vec{E}_+ + \vec{E}_- = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r} - \frac{Q}{4\pi\epsilon_0 r^2} \left(\frac{r^4}{R^4} \right) \hat{r} \\ &= \frac{Q}{4\pi\epsilon_0 r^2} \left(\frac{R^4 - r^4}{R^4} \right) \hat{r} \end{aligned}$$

e. The electric potential V inside the sphere at a distance $r<R$ from the center

$$\text{当 } r < R \text{ 时 } +Q \text{ 产生的势能 } V_+ = \frac{Q}{4\pi\epsilon_0 r}$$

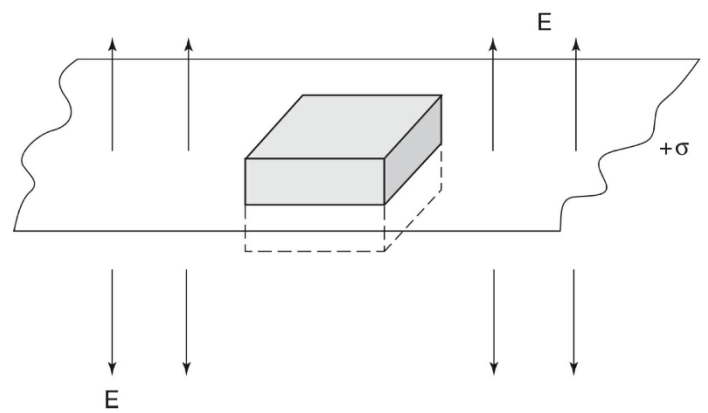
$$\text{当 } r < R \text{ 时 } -Q \text{ 的势能 } V_- = \frac{-Q}{4\pi\epsilon_0 r} \frac{r^4}{R^4}$$

$$\begin{aligned} \Sigma V &= V_+ + V_- = \frac{Q}{4\pi\epsilon_0 r} - \frac{Q}{4\pi\epsilon_0 r} \frac{r^4}{R^4} \\ &= \frac{Q}{4\pi\epsilon_0 r} \frac{R^4 - r^4}{R^4} \end{aligned}$$

Gauss's Law 高斯定律

Gauss's Law	电通量: Φ_{net}	$\Phi_{net} = \oint_s \vec{E} \cdot \vec{n}dA = \oint_s E_n dA$
	当 Φ 均匀分布时	$\Phi_{net} = E_n A = \frac{Q_{in}}{\epsilon_0}$
考点:	<ul style="list-style-type: none"> 通量的概念: 垂直于某个表面的量称为通量 \Rightarrow 电通量定义 均匀电场 \Rightarrow 高斯面上电通量均匀 \Rightarrow 高斯定律算通量或电场 Φ_{net}: 穿过高斯表面的净 flux \Rightarrow 和此表面上的电荷注意区分 Q_{in}: 高斯面里面的净 charge 	

Example: (Barron P420) Calculate the electric field produced by an infinitely large sheet of charge with uniform charge density $+\sigma$ C/m².

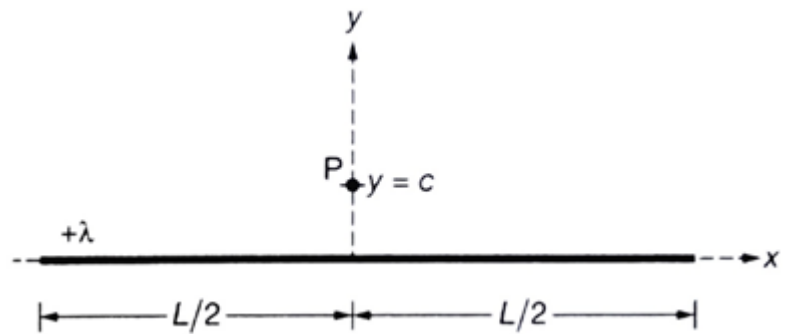


上下各一个 Gaussian surface: $A = x \times y$, 总面积 $2A$
The enclosed charge: $Q_{in} = \sigma A$

Gauss's Law: (当 Φ 均匀分布时) $\Phi_{net} = E_n A = \frac{Q_{in}}{\epsilon_0}$

$$E_n(2A) = \frac{\sigma A}{\epsilon_0} \Rightarrow E_n = \frac{\sigma}{2\epsilon_0}$$

Example: (APC HW13-9) A very long, thin, nonconducting cylinder of length L is centered on the y -axis, as shown. The cylinder has a uniform linear charge density $+\lambda$. Point P is located on the y -axis at $y=c$, where $L \gg c$. Setup a Gaussian surface and use it to calculate the magnitude of the electric field at point P in terms of λ , c , L and physical constants.

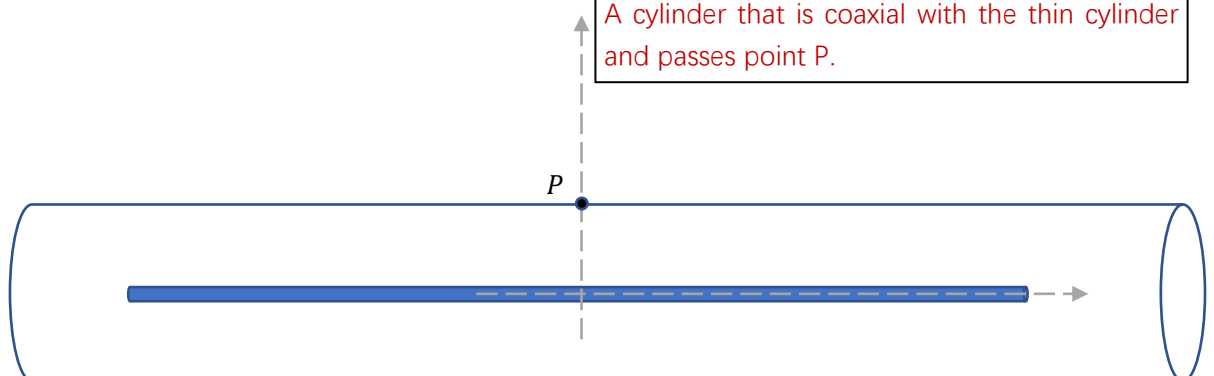


A cylinder that is coaxial with the thin cylinder and passes point P .

Gauss's law: $\frac{q_{inside}}{\epsilon_0} = \int E dA \Rightarrow \frac{Q}{\epsilon_0} = EA$

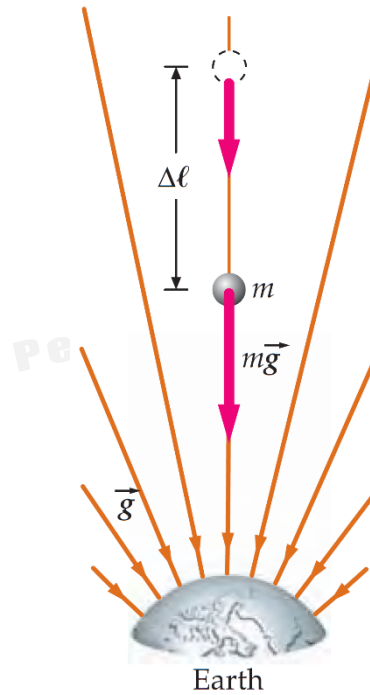
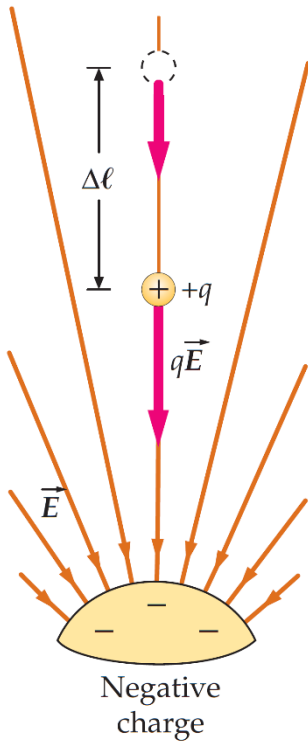
$$\left. \begin{matrix} A \approx (2\pi c)L \\ Q = \lambda L \end{matrix} \right\} \Rightarrow \frac{\lambda L}{\epsilon_0} = E(2\pi cL)$$

$$\Rightarrow E = \frac{\lambda}{2\pi c \epsilon_0}$$



Potential and Electric Field 电场和重力场(p765)

Charge q	mass m
Coulomb's Law $F = \frac{k q_1q_2 }{r^2}$ $k = 8.99 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$	The Universal Gravitation $F_g = \frac{Gm_1m_2}{r^2}$ $G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
Electric Field $\vec{F} = q\vec{E}$ $E = \frac{kQ}{r^2}$	Gravitational Field $\vec{F} = m\vec{g}$ $g = \frac{GM_e}{r^2}$
Electric Potential Energy $U_e = VQ$	Gravitational Potential Energy $U_m = mgh$
Potential Difference $V = \frac{U_e}{q} = -\vec{E} \cdot \vec{l}$	Height Difference $h = \frac{U_m}{mg}$



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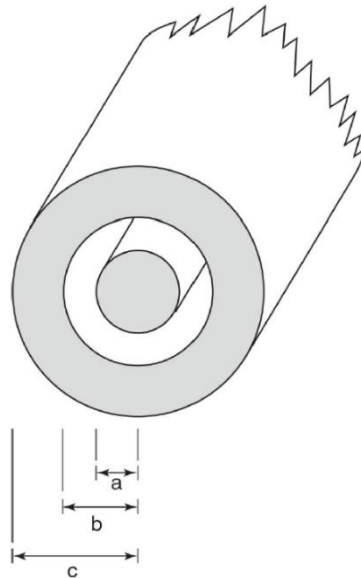
Capacitance 电容

- Capacitance: $C = Q/V$
 Isolated spherical conductor $C = 4\pi\epsilon_0 R$
 Parallel-plate capacitor $C = \epsilon_0 A/d$
- Energy in Capacitors: $dU = VdQ = QdQ/C \Rightarrow U = \int \frac{Q}{C} dQ = \frac{Q^2}{2C}$
 $U = \frac{1}{2} QV = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} CV^2$
- Dielectrics: $C = kC_0 \quad \epsilon = k\epsilon_0$
 $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$
- Equivalent Capacitance:
 Parallel capacitors $C_{eq} = C_1 + C_2 + C_3 + \dots$
 Series capacitors $1/C_{eq} = 1/C_1 + 1/C_2 + 1/C_3 + \dots$

Calculating Capacitance Based on Geometry: $C = Q/\Delta V$

- 计算 E \leftarrow 当 Φ 均匀分布时 $\Phi_{net} = EA$
- 计算 ΔV \leftarrow $dV = -\vec{E} \cdot d\vec{l}$
- 计算 C \leftarrow $C = Q/\Delta V$

Example: Consider the coaxial cable in the right figure, which contains a central cylindrical core of metal (radius a) surrounded by a cylindrical sheath of metal (inner radius b, outer radius c). Charge is moved from the sheath to the inner cylinder, so that charge density is then λ coulombs/length along the inner cylinder and $-\lambda$ along the sheath.



What is the capacitance of a coaxial cable of length l (ignore edge effects, as in our treatment of a parallel plate capacitor).

Step 1: 计算 E

在 $a < r < b$ 的位置, 设置同轴高斯面

$$\Phi_{net} = \oint_s E_n dA \xrightarrow{E \perp A} \Phi_{net} = EA$$

$$\Phi_{net} = E(2\pi r \cdot l) = \frac{Q_{in}}{\epsilon_0} = \frac{\lambda l}{\epsilon_0}$$

$$E = \frac{\lambda}{2\pi r \epsilon_0}$$

Step 2: 计算 ΔV

$$V_b - V_a = \int_a^b dV = - \int_a^b E dr = - \int_a^b \frac{\lambda}{2\pi r \epsilon_0} dr = \frac{\lambda}{2\pi \epsilon_0} \ln \frac{a}{b}$$

Step 3: $C=Q/\Delta V$

$$C = \frac{Q}{\Delta V} = \frac{\lambda l}{|V_b - V_a|} = \frac{2\pi \epsilon_0 l}{\ln \frac{a}{b}}$$